

I'm not a bot

























[illegible]

plane with 13 points which looks just like to the diagram I made for 13 cards of four symbols. Unfortunately, I don't think there is a nice diagram for arranging 13 points and 13 lines. Getting back to the empirical approach, we can continue to increase the number of symbols to see if any more patterns emerge. With eight symbols, we have a similar situations as with four symbols. We need more than three symbols per card because three symbols are maxed out by seven cards. But with four symbols, two cards don't cover all the symbols (requirement 5), and with three cards, there's not enough symbols. With five or more symbols, the overlap between two cards is too great. With nine symbols we do now have space for three cards of four symbols. With ten symbols we have the fifth triangular number, and so can get five cards of four symbols. Since this is a triangular number each symbol appears on exactly two cards. ABCD AEFG BEHI CFHJ DGJI ABCD AEFG BEHI CFHJ DGJI A B C D E F G H I J A B C D E F G H I J We can keep going.

plotting the results on a graph. Notice the series of peaks at the Dobble numbers, each one having  $k = n$ . Total symbols (n) Maximum number of cards (k) 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 1 5 9 13 17 21 Following each Dobble number, when  $n = D(s) + 1$ , the value of  $k$  crashes. For the first three "Dobble plus one" numbers (\$2\$, \$4\$ and \$8\$), the deck size is one. With 14 symbols we finally have enough symbols to scrape four cards together. The numbers \$2\$, \$4\$ and \$8\$ are also powers of two. With 16 symbols, we have the first power of two, which is not a "Dobble plus one" number. With 16 symbols we can make six cards, which is a lot better than one. However we can also make six cards with 15 symbols (a triangular number). This is the only example so far where increasing  $n$  doesn't increase  $k$  other than the "Dobble plus one" numbers. So it seems that it's hard to make decks when  $n$  is a power of two. Another interesting parameter to look at is the mean number of times each symbol appears in a deck,  $r$ . For example with nine symbols, we had the cards \$ABCD\$, \$AEFG\$ and \$BEHI\$. So \$A\$, \$B\$ and \$E\$ appear twice, while the remaining six symbols appear once. Therefore  $r = \frac{3 \times 2 + 6 \times 1}{9} = \frac{4}{3}$ . Total symbols (n) Mean symbol repeats (r) 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 1 2 3 4 5 Perhaps unsurprisingly, this graph has a similar shape to before since the more cards in a deck, the more each symbol is repeated. One small difference is that now there is a dip at  $n = 16$  rather than a flat line. A more interesting trend becomes apparent when we look at values for which  $r$  is an integer. We already know when  $n$  is a triangular number,  $r = 2$ , and when  $n$  is the Dobble number,  $r = s$  (\$21\$ is both a triangular number and a Dobble number, but the Dobble number wins out since we want the largest deck). The first four powers of two, \$1\$, \$2\$, \$4\$ and \$8\$, all have one card, so  $r = 1$ . Dobble minus one There is one other type of number that has an integer value for  $r$ : the "Dobble minus one" numbers. When  $n$  is one less than a Dobble number, the number of repeats is one less than for that Dobble number, i.e if  $n = D(s) - 1$ , then  $r = s - 1$ . With  $n = D(2) - 1 = 2$ ,  $r = 1$  With  $n = D(3) - 1 = 6$ ,  $r = 2$  With  $n = D(4) - 1 = 12$ ,  $r = 3$  With  $n = D(5) - 1 = 20$ ,  $r = 4$  This is just an empirical observation, based on these four (five if you include  $D(1) - 1 = 0$ ) values. I don't have yet have any proof or any sense of the logic for why this might be the case (assuming the pattern holds). The total number of symbols in a deck is equal to the number of symbols multiplied by the average number of repeats. So if this pattern does hold, the total number of symbols in these decks,  $n$ , is: 
$$n = (D(s) - 1) \cdot (s - 1) \vee n = (s^2 - s) \cdot (s - 1) \vee n = s^3 - 2s^2 + s$$
 The number of cards in a deck,  $k$ , is equal to the total number of symbols divided by the number of symbols per card: 
$$k = \frac{n}{s} = \frac{(s^3 - 2s^2 + s)}{s} = s^2 - 2s + 1 \vee k = (s - 1)^2$$
 Conjecture: If the number of symbols,  $n$ , is in the form  $s(s - 1)$ , then  $k = (s - 1)^2$ . e.g  $n = 12 = 4 \times 3$ , so  $k = 3^2 = 9$  Once the deck size gets into the teens, it becomes hard to be sure that you've found the best solution using pen and paper. So I built a tool to help me. It keeps track of which cards you've matched and stops you from adding symbols found on matched cards. This means a lot of the work is done for you and often only have to worry about picking the correct first symbol for each card. To find even larger decks I tried to write a program to find decks by brute force, trying all valid solutions. Sadly, I think it worked in  $O(n!)$  time or worse, so by the time I reached  $n = 12$  it was taking too long to run. There's probably a lot I could do to improve its efficiency, but I think I need a more clever strategy to get anything useful. I think that looking at the number of times each symbol is repeated as the deck is built might yield something, but I haven't worked out the specifics. The real game of Dobble has 55 cards with eight symbols on each card. The eighth Dobble number is  $D(8) = 8^2 - 8 + 1 = 57$  so they could have had two more cards. I guess they decided 57 didn't seem like such a nice number. Presumably there are then 15 (\$8 + 7\$) symbols that appear only seven times. The Dobble Kids version has six symbols per card and "30 cards with more than 30 paper animals". More than 30 paper animals must refer to the fact that there are 31 (\$D(6)\$) different symbols. The Mathematics of Toys and Games

**What type of game is dobbble. Is dobbble a good game. How does the game dobbble work. Dobble kaartspel. What is dobbble card game. Dobble spelregels. Dobble uitleg. What are the 5 dobbble games. Dobble speluitleg.**