

I'm not a robot



amount of energy needed to change a sample of a substance of mass m from a solid or liquid or vice versa without any change in its temperature is proportional to its mass with the following formula $Q = \rho m \Delta T$ where ρ is called the latent heat of fusion of that substance. Plus sign indicates that heat must be added to the substance during the melting process. Minus sign shows that heat must be removed from the substance during the freezing process. The SI units of latent heat of fusion are J/kg or cal/kg . It is also known as the enthalpy of fusion. The latent heat of fusion of water is 333.5 J/kg . This number indicates that to melt one kilogram of solid water into liquid water, we must extract 333.5 J/kg heat from the ice. In all heat problems, first, identify whether there is a temperature change or not. If there was, then use the equation $Q = mc\Delta T$ to solve the unknown. If not, then read this article. Further solving: Specific heat problems with answers Heat examples problems with solutions Latent Heat of Fusion Example Problems with Answers: Problem (1): How much heat is needed to change 2 kg of ice at 0°C to 100°C of water? (specific heats of ice and water are $2.09 \text{ J/kg}^\circ\text{C}$ and $4.18 \text{ J/kg}^\circ\text{C}$, respectively) Solution: This is the simplest example of a latent heat problem. The total heat needed to change ice into steam breaks into four parts: Q_1 is the heat required to change its temperature from 0°C to 100°C of ice $Q_1 = m c_{\text{ice}} \Delta T = 2 \text{ kg} \times 2.09 \text{ J/kg}^\circ\text{C} \times 100^\circ\text{C} = 418 \text{ J}$. Q_2 is the heat needed to melt the ice or phase change, $Q_2 = m L_f = 2 \text{ kg} \times 333.5 \text{ J/kg} = 667 \text{ J}$. Q_3 is the heat required to increase the temperature from 100°C to 100°C of water $Q_3 = m c_{\text{water}} \Delta T = 2 \text{ kg} \times 4.18 \text{ J/kg}^\circ\text{C} \times 0^\circ\text{C} = 0 \text{ J}$. Q_4 is the heat required to increase the temperature from 100°C to 100°C of steam $Q_4 = m c_{\text{steam}} \Delta T = 2 \text{ kg} \times 2.09 \text{ J/kg}^\circ\text{C} \times 0^\circ\text{C} = 0 \text{ J}$. The total heat needed is $Q = Q_1 + Q_2 + Q_3 + Q_4 = 418 \text{ J} + 667 \text{ J} + 0 \text{ J} + 0 \text{ J} = 1085 \text{ J}$. Problem (2): How much heat is needed to transform 2 kg of ice at 0°C to 100°C of water? (specific heats of ice and water are $2.09 \text{ J/kg}^\circ\text{C}$ and $4.18 \text{ J/kg}^\circ\text{C}$, respectively) Solution: first, the 2 kg of ice at 0°C must absorb the following heat Q_1 to reach 100°C of ice $Q_1 = m c_{\text{ice}} \Delta T = 2 \text{ kg} \times 2.09 \text{ J/kg}^\circ\text{C} \times 100^\circ\text{C} = 418 \text{ J}$. Then, it must transform into 100°C of water by absorbing the heat Q_2 to below 100°C of water $Q_2 = m L_f = 2 \text{ kg} \times 333.5 \text{ J/kg} = 667 \text{ J}$. In the final stage, the heat Q_3 is needed to increase the temperature of the water (melted ice) to 100°C of water $Q_3 = m c_{\text{water}} \Delta T = 2 \text{ kg} \times 4.18 \text{ J/kg}^\circ\text{C} \times 0^\circ\text{C} = 0 \text{ J}$. The total heat needed is $Q = Q_1 + Q_2 + Q_3 = 418 \text{ J} + 667 \text{ J} + 0 \text{ J} = 1085 \text{ J}$. Problem (3): How much heat is needed to transform 2 kg of ice at 0°C to 100°C of water? (specific heats of ice and water are $2.09 \text{ J/kg}^\circ\text{C}$ and $4.18 \text{ J/kg}^\circ\text{C}$, respectively) Solution: first, the 2 kg of ice at 0°C must absorb the following heat Q_1 to reach 100°C of ice $Q_1 = m c_{\text{ice}} \Delta T = 2 \text{ kg} \times 2.09 \text{ J/kg}^\circ\text{C} \times 100^\circ\text{C} = 418 \text{ J}$. Then, it must transform into 100°C of water by absorbing the heat Q_2 to below 100°C of water $Q_2 = m L_f = 2 \text{ kg} \times 333.5 \text{ J/kg} = 667 \text{ J}$. In the final stage, the heat Q_3 is needed to increase the temperature of the water (melted ice) to 100°C of water $Q_3 = m c_{\text{water}} \Delta T = 2 \text{ kg} \times 4.18 \text{ J/kg}^\circ\text{C} \times 0^\circ\text{C} = 0 \text{ J}$. The total heat needed is $Q = Q_1 + Q_2 + Q_3 = 418 \text{ J} + 667 \text{ J} + 0 \text{ J} = 1085 \text{ J}$. Problem (4): How much heat is needed to transform 2 kg of ice at 0°C to 100°C of water? (specific heats of ice and water are $2.09 \text{ J/kg}^\circ\text{C}$ and $4.18 \text{ J/kg}^\circ\text{C}$, respectively) Solution: first, the 2 kg of ice at 0°C must absorb the following heat Q_1 to reach 100°C of ice $Q_1 = m c_{\text{ice}} \Delta T = 2 \text{ kg} \times 2.09 \text{ J/kg}^\circ\text{C} \times 100^\circ\text{C} = 418 \text{ J}$. Then, it must transform into 100°C of water by absorbing the heat Q_2 to below 100°C of water $Q_2 = m L_f = 2 \text{ kg} \times 333.5 \text{ J/kg} = 667 \text{ J}$. In the final stage, the heat Q_3 is needed to increase the temperature of the water (melted ice) to 100°C of water $Q_3 = m c_{\text{water}} \Delta T = 2 \text{ kg} \times 4.18 \text{ J/kg}^\circ\text{C} \times 0^\circ\text{C} = 0 \text{ J}$. The total heat needed is $Q = Q_1 + Q_2 + Q_3 = 418 \text{ J} + 667 \text{ J} + 0 \text{ J} = 1085 \text{ J}$. Problem (5): How much heat is needed to transform 2 kg of ice at 0°C to 100°C of water? (specific heats of ice and water are $2.09 \text{ J/kg}^\circ\text{C}$ and $4.18 \text{ J/kg}^\circ\text{C}$, respectively) Solution: first, the 2 kg of ice at 0°C must absorb the following heat Q_1 to reach 100°C of ice $Q_1 = m c_{\text{ice}} \Delta T = 2 \text{ kg} \times 2.09 \text{ J/kg}^\circ\text{C} \times 100^\circ\text{C} = 418 \text{ J}$. Then, it must transform into 100°C of water by absorbing the heat Q_2 to below 100°C of water $Q_2 = m L_f = 2 \text{ kg} \times 333.5 \text{ J/kg} = 667 \text{ J}$. In the final stage, the heat Q_3 is needed to increase the temperature of the water (melted ice) to 100°C of water $Q_3 = m c_{\text{water}} \Delta T = 2 \text{ kg} \times 4.18 \text{ J/kg}^\circ\text{C} \times 0^\circ\text{C} = 0 \text{ J}$. The total heat needed is $Q = Q_1 + Q_2 + Q_3 = 418 \text{ J} + 667 \text{ J} + 0 \text{ J} = 1085 \text{ J}$. Problem (6): How much heat is needed to transform 2 kg of ice at 0°C to 100°C of water? (specific heats of ice and water are $2.09 \text{ J/kg}^\circ\text{C}$ and $4.18 \text{ J/kg}^\circ\text{C}$, respectively) Solution: first, the 2 kg of ice at 0°C must absorb the following heat Q_1 to reach 100°C of ice $Q_1 = m c_{\text{ice}} \Delta T = 2 \text{ kg} \times 2.09 \text{ J/kg}^\circ\text{C} \times 100^\circ\text{C} = 418 \text{ J}$. 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Then, it must transform into 100°C of water by absorbing the heat Q_2 to below 100°C of water $Q_2 = m L_f = 2 \text{ kg} \times 333.5 \text{ J/kg} = 667 \text{ J}$. In the final stage, the heat Q_3 is needed to increase the temperature of the water (melted ice) to 100°C of water $Q_3 = m c_{\text{water}} \Delta T = 2 \text{ kg} \times 4.18 \text{ J/kg}^\circ\text{C} \times 0^\circ\text{C} = 0 \text{ J}$. The total heat needed is $Q = Q_1 + Q_2 + Q_3 = 418 \text{ J} + 667 \text{ J} + 0 \text{ J} = 1085 \text{ J}$. Problem (8): How much heat is needed to transform 2 kg of ice

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C)\end{align*} Problem (6): When 3 kg of water is cooled from 80°C to 10°C, how much heat energy is lost? (specific heat of water is $c_w=4.179\text{ J/g}\cdot^\circ\text{C}$)\$ Solution: the heat has led to a change in temperature, so we must use the formula $Q=mc\Delta T$ to find the lost heat as shown below: \begin{align*} Q&=mc(T_f-T_i)\\&=3000\times 4.179\times (10^\circ\text{C}-80^\circ\text{C})\\&=-877590\text{ J} \end{align*} Note that in the above calculation, the specific heat capacity is given in $\text{J/g}\cdot^\circ\text{C}$, and the mass of water is in kilograms. Therefore, first convert mass into grams or use consistent units throughout the calculation. Here, we converted 3 kg to 3000 g. The negative sign indicates that the heat is released from the water. Problem (7): Calculate the temperature change when: (a) 10.0 kg of water loses 232 kJ of heat. ($c_w=4.179\text{ J/g}\cdot^\circ\text{C}$)\$ (b) 8954 J of heat is added to 3 moles of copper. ($c_{\text{Cu}}=0.385\text{ J/g}\cdot^\circ\text{C}$)\$ Solution: In both parts, we use the heat formula for temperature changes, $Q=mc(T_f-T_i)$ \$. (a) Substituting known values $m=10\text{ kg}$ and $Q=-232\text{ kJ}$ (note the negative sign for heat loss) into the equation and solving for the change in temperature $\Delta T=T_f-T_i$ is: \begin{align*} \Delta T&=\frac{Q}{mc}\\&=\frac{-232000}{10\times 4179}\\&=-5.55^\circ\text{C} \end{align*} Since the water loses heat energy (hence the negative sign for Q), its temperature decreases. Here, 5.55 kJ (kilojoules) is converted to 5550 J by multiplying by 1000. (b) The molar mass of copper M is 63.5 g/mol . Therefore, the mass of 3 moles of copper is calculated as follows: \begin{align*} m&=n\times M\\&=3\times 63.5\text{ g}\\&=190.5\text{ g} \end{align*} Next, we find the temperature increase using the heat equation: \begin{align*} \Delta T&=\frac{Q}{mc}\\&=\frac{8954}{190.5\times 0.385}\\&=119^\circ\text{C} \end{align*} Thus, the temperature increase of the copper is 119°C . Problem (8): A 180-gram sample of an unknown material is heated to 280°C . This hot sample is then immediately submerged into a 95-gram copper calorimeter containing 150 grams of water and a 12-gram glass thermometer. The initial temperature of the calorimeter, water, and thermometer is 20.0°C . After reaching thermal equilibrium, the final temperature of the system is 32.5°C . Determine the specific heat of the unknown material. (Assume no heat is lost to the surroundings.) Solution: These types of problems fall under calorimetry. In such cases, some objects lose heat while others gain it until they reach thermal equilibrium at a specific final temperature. In this question, the unknown material (x) at a higher temperature of 280°C loses its heat energy to reach the equilibrium temperature of 32.5°C . The other components at a lower temperature gain this heat. According to the energy conservation principle (or in this case, the principle of calorimetry), we have $Q_{\text{gain}}=-Q_{\text{lost}}$. The negative sign ensures that the right side has a positive value. Therefore, \begin{align*} Q_{\text{lost}}&=mc\Delta T\\&=(0.180\text{ kg})(32.5^\circ\text{C}-280^\circ\text{C})\\&=-44.55\text{ kJ} \end{align*} And the heat gained by other components is given by: $Q_{\text{gain}}=(m_w c_w + m_c c_c + m_g c_g) \Delta T$. Substituting the given values, we find the heat gained by these objects: $Q_{\text{gain}}=8420.7\text{ J}$. Therefore, using energy conservation: \begin{gather*} Q_{\text{gain}}=-Q_{\text{lost}}\\8420.70=44.55\times x \end{gather*} \Rightarrow x\approx 189\text{ J/g}\cdot^\circ\text{C} Therefore, the specific heat of the unknown material is approximately $189\text{ J/g}\cdot^\circ\text{C}$. Author: Dr. Ali Nemati Page Created: 3/9/2021 Share — copy and redistribute the material in any medium or format for any purpose, even commercially. Adapt — remix, transform, and build upon the material for any purpose, even commercially. The licensor cannot revoke these freedoms as long as you follow the license terms. Attribution — You must give appropriate credit , provide a link to the license, and indicate if changes were made . You may do so in any reasonable manner, but not in any way that suggests the licensor endorses you or your use. ShareAlike — If you remix, transform, or build upon the material, you must distribute your contributions under the same license as the original. No additional restrictions — You may not apply legal terms or technological measures that legally restrict others from doing anything the license permits. You do not have to comply with the license for elements of the material in the public domain or where your use is permitted by an applicable exception or limitation . No warranties are given. The license may not give you all of the permissions necessary for your intended use. For example, other rights such as publicity, privacy, or moral rights may limit how you use the material. 0 ratings0% found this document useful (0 votes)1K viewsThis document contains 14 problems related to concepts of heat transfer, phase changes, and thermodynamics. The problems involve calculating heat transfer, temperature changes, energy requir...AI-enhanced title and description